A Comparative Study of Failure Data for Software Reliability Estimation

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Abstract
Software reliability is one of the attributes of quality and its measurement is supported by Software Reliability Growth Models. Among many of the proposed SRGMs, some of the models have been widely used and few of them obsolete. The successful SRGMs are characterized by the accuracy of reliability estimation. In such models, the reliability estimation depends on the quality of failure data and its accuracy increases as the length of failure observation increases. In this paper, we have studied the role of failure data set in the reliability estimation by employing three different data sets on unified SRGM that has no distinction between failure observation and fault removal process. The selected SRGM is incorporated with two distribution functions one is exponential and another one is 2-staged erlang distribution. For easy implementation, we assume that the debugging process is perfect. That is the probability of error correction is one and no errors have been introduced during the debugging process. Three different cases of failure data are considered for our study such as database application software, web server, the interface of an operating system. The unknown parameters of each case are estimated by using SMERFS tool and the goodness-of-fit analysis is done in MATLAB environment.

Keywords
Fault Count Data, Software Reliability Growth Model, Failure Intensity Function, Software Reliability Function, Non-Homogeneous Poisson Process

Acronym
TNOFR Total Number of Faults Remaining

TNOF Total Number of Faults
RF Reliability Factor
SSE Sum of Squared Error
RMSE Root Mean Square Error
SMERFS Statistical Modeling and Estimation of Reliability Functions

Notation
m(t) mean value function
λ(t) Failure Intensity function
λ(t+δx) Failure Intensity function for the next δx time units
m(t+δx) mean value function for the next δx time units
R(t | δx) Reliability function for the next δx time units
b(t) Failure detection rate
a initial number of faults
b proportionality constant
p probability of error generation
α error generation rate
δ failure time / failure interval
Σ_{i=1}^n f_i total number of faults observed at n time intervals
\bar{f}_n \text{ n}^{th} time interval
\bar{f} mean of the observed faults
f_i faults observed at i^{th} time

I. Introduction
Software failures have been formally classified with respect to their criticality to the system operation and maintenance as expected failures, configuration failures and critical failures [8]. Expected failures are caused by frequent system start, frequent migration, system update and unplanned code re-engineering. These failures could be managed by using appropriate documents and schedules. The second class of failures is configuration failures which are caused by incomplete installation, incompatible environment and version conflicts within the system. This can be addressed by having proper configuration control and management. The third class of failures is critical failures that need consistent solution. Since the causes of such failures are unexpected, there is need for a model based mechanism to forecast

- System crashes
- Hardware failures
- Failures in application associations and linkages
- Violations in communication and interfaces

In order to address the above issues, many SRGMs have been proposed in the literature. Reliability models predict the intensity of failure and the cumulative number of faults at the specified time instant. With respect to time instant whether calendar time or CPU execution time, software failure data are classified into Time Between Failure Data and Fault Count Data. The former class of failure data is described by the test interval and the later class of failure data is described by the fault count at the specified time instant. The SRGMs for each class of failure data differ by their initial assumptions [5].

Poisson process models are used to describe the occurrences of random failures during the testing phase [13]. The failure counting process is characterized by the failure rate represented by the parameter say λ. In practical, software failure rate is non-linear, the failure counting process is modeled by Non-Homogeneous Poisson Process given in [1]

\[ P = \frac{e^{-\lambda t}}{k!} \lambda^k, \quad k = 0, 1, 2, \ldots \]  \hspace{1cm} (1)

Two versions of unified SRGM models have been proposed and we select generalized NHPP model that treats both failure observation and fault removal process as same function. The first version of unified SRGM in given in [1] as follows

\[ m(t) = a \left[ \frac{1}{1 - \alpha} \left( 1 - (1 - F(t))^{(1-\alpha)} \right) \right] \]  \hspace{1cm} (2)

In the above model, F(t) is the generalized representation of failure observation or fault removal process and there is no distinction between failure observation process and fault removal process. We employ two failure distribution functions, the exponential and two-staged erlang distribution into the F(t) of (2) to derive NHPP model and delayed S-shaped model. For the derivation purpose, we have the following assumptions on (2)
Similarly, the two-staged Erlang distribution is given by

\[ F(t) = 1 - e^{-bt} \]  

Now (3) is incorporated in (2) then we have

\[ m(t) = \frac{a}{1-\alpha} \left[ 1 - e^{-bp(1-\alpha)t} \right] \]  

Similarly, the two-staged Erlang distribution is given by

\[ F(t) = 1 - (1 + bt)e^{-bt} \]  

which is incorporated in (2) we have

\[ m(t) = \frac{a}{1-\alpha} \left[ 1 - ((1 + bt)e^{-bt})^p(1-\alpha) \right] \]  

By using the model assumptions such as \( \alpha=0 \) and \( p=1 \) then the (4) and (6) becomes

\[ m(t) = a(1 - e^{-bt}) \]  

\[ m(t) = a[1 - ((1 + bt)e^{-bt})] \]  

Here (7) represents NHPP SRGM model and (8) represents delayed S-shaped model. Table 1 summarizes the characteristics of both NHPP and Delayed S-shaped SRGM models [1].

Table 1: Summary of selected two SRGMs

<table>
<thead>
<tr>
<th>Model Name</th>
<th>Mean Value Function ( m(t) )</th>
<th>Failure Intensity Function ( \lambda(t) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>NHPP Model</td>
<td>( a(1-e^{bt}) )</td>
<td>( abe^{bt} )</td>
</tr>
<tr>
<td>S-shaped Model</td>
<td>( a[1-(1+bt)e^{bt}] )</td>
<td>( ab^2te^{bt} )</td>
</tr>
</tbody>
</table>

A. Parameter Estimation

For both models, the proportionality constant is estimated by using specific tool SMERFS 3.0 and the other parameter is computed using MLE functions. The first parameter represents initial number of faults at the start of failure observation and the second proportionality constant parameter represents failure rate that occurs during the failure observation. For each data set and each model, the value of proportionality constant is obtained from SMERFS output. By using the value of proportionality constant that is obtained for each SRGM model and for each Data Set, the initial faults can be computed for each model. For NHPP models the value is obtained by using (9) and for delayed S-shaped model the value is obtained by using (10).

\[ a = \frac{\sum_{i=1}^{n} f_i}{(1- e^{-btn})} \]  

(9)

\[ a = \frac{\sum_{i=1}^{n} f_i}{1-(1+btn)e^{-btn}} \]  

(10)

After obtaining the values of unknown parameters of the two selected SRGM models, their \( \lambda(t) \), \( m(t) \) are computed. The failure intensity function describes the faults residuals and the mean value function of each model describes the expected number of faults at each time instant within the length of failure observation. By using \( m(t) \) of each model, the reliability function \( R(t | \delta x) \) is computed as follows

\[ R(t | \delta x) = e^{-(m(t+\delta x)-m(t))} \]  

(11)

II. Related Work

A set of software metrics have been proposed to account for information gained from a user’s point view regarding the severity of the observed failures. By adapting such metric set, an extended Modified Adaptive Strategy (MAT) has been proposed for better estimation of reliability [14]. A generalized SRGM model has been proposed based on the classification of the faults with respect to their removal complexities. This model addresses the problems in the imperfect debugging and error generation rate and supports for realistic estimation [11]. A scheme has been proposed for constructing SRGM based on NHPP where testing effort is described as Generalized Exponential Distribution (GED) with the assumption that the error detection rate is proportional to the current fault content [12]. Software Testing strategies have been analyzed with respect to the attained failure size to reveal the impact of software testing effort and the failure data volume [9]. The importance of residuals and the total number of expected faults which are taken into account for the measurement of software reliability is addressed in [6,8]. Both fault detection and removal process are integrated and a new SRGM has been modeled based on the integration in [3,7]. A quantitative approach for the measurement of reliability on open source software systems has been proposed and analyzed to address the issues on the optimal release policies. The measurement of reliability has been studied and implemented on two open source software systems MySQL and Linux Kernel [4,15-16]. A Unified approach has been incorporated for fault modeling and two versions of unified SRGM model have been proposed by incorporating both imperfect debugging and error generation. The first version of unified SRGM has no distinction between failure observation and fault removal and the second version models both are different. Both versions of unified SRGMs have good applicability by supporting many of the failure distributions [1-2].

III. Data Analyses

Three data sets have been taken for the comparative analysis of software reliability estimation. DS-I represents the failure data obtained from PL/I database application software where 328 faults have been reported in 19 weeks [3]. The remaining two data sets DS-II and DS-III have been obtained from famous OSS projects...
of their first release. DS-II represents failure data of GNOME project of its first version 2.0 where 74 faults have been reported in 24 weeks [4]. DS-III represents failure data of Apache project of its first version 2.0.35 where 85 faults have been reported in 35 days [4].

A. Model Validation
Both models can be validated on the given three data sets using curve fit analysis. The following criteria have been taken in account to understand the goodness of fit for three data sets to be employed with both NHPP model and Yamada S-shaped model.

1. SSE (Sum of Squared Error)
It is the sum of squared difference between the estimated curve and the actual data. The smaller value of SSE indicates better fit. It is defined in [1] as

\[ SSE = \sum_{i=1}^{n} (f_i - m(t_i))^2 \]  

(12)

2. R^2 (R-Square)
It is the ratio of sum of squared in the regression about the mean. The R2 value can take any value between 0 and 1 where the value which is closer to 1 has better fit. It is defined in [1] as

\[ R^2 = 1 - \frac{\sum_{i=1}^{n}(m(t_i) - \bar{f})^2}{\sum_{i=1}^{n}(f_i - \bar{f})^2} \]  

(13)

3. RMSE (Root Mean Square Error)
It is the measure of closeness with which the model prediction and the observation. The lower value indicates better fit. It is defined in [1] as

\[ Bias = \frac{\sum_{i=1}^{n}(m(t_i) - f_i)}{n} \]  

(14)

\[ RMSE = \sqrt{Bias^2 + Variance^2} \]  

(15)

\[ Var = \frac{1}{n-1} \sum_{i=1}^{n} (f_i - m(t_i) - Bias)^2 \]  

(16)

For DS-I, S-shaped model (M-II) has better fit than NHPP (M-I) model. For DS-II and DS-III, a negative R2 was generated in NHPP model which shows non-applicability of R2 and remaining criteria of goodness of fit are same in both NHPP and S-shaped models. To avoid negative R2 value, data set has to be normalized to some measurement unit. Table 2 to 4 shows the goodness of fit analysis of three data sets on two SRGM models M-I and M-II.

| Table 3: Curve fit analysis for DS-II |
|-------------------|-----|-----|-----|-----|
| DS – II           |     |     |     |
| A   | B   | SSE | R^2 | RMSE |
| M-I | 118.0999 | 0.053 | 142 | NA   | 2.54 |
| M-II| 91.2064  | 0.182 | 142 | NA   | 2.54 |

| Table 4: Curve fit analysis for DS-III |
|-------------------|-----|-----|-----|-----|
| DS – III          |     |     |     |
| A   | B   | SSE | R^2 | RMSE |
| M-I | 87.7248 | 0.053 | 133.5 | NA | 2.012 |
| M-II| 76.5093  | 0.15 | 133.5 | 2.22E-16 | 2.012 |

IV. Model Performance Analysis
The performance of both models on the given three data sets has been illustrated graphically by using MATLAB 9.0. Each data set is employed with both NHPP and delayed S-shaped model to generate m(t) and failure intensity plots. From each plot, we describe the performance as follows;

A. Data Set-I
1. m(t) is better for NHPP model than Yamada S-shaped model. At m(tn), the prediction plot of NHPP model is very close to the total number faults where as plot of S-shaped model deviated as in fig. 1(a)

\[ \lambda(t) \] is constantly decreases as time increases for NHPP model whereas failure intensity increases and then decreases than NHPP model because Yamada S-shaped model considers the delay between failure observation and fault removal as in fig. 1(b). The reduced failure intensity has good estimate of reliability.

Fig. 1(a) Mean Value Function Plot for DS-I
Fig. 1(b): Failure Intensity Plot for DS-I
B. Data Set-II
1. At the start of failure observation, \( m(t) \) for both NHPP and Yamada S-shaped models is very close to each other and then considerably deviates at \( m(tn) \) as in fig. 2(a)
2. Alternately \( \lambda(t) \) for both models have deviation and close to each other at \( m(tn) \) as in fig. 2(b)

C. Data Set-III
1. At \( m(t_1) \), the prediction plot for both models are closer together, but have much deviation at \( m(t_n) \) as graphically illustrated in fig. 3(a).
2. The failure intensity at both \( m(t_1) \) and \( m(t_n) \) are closer for each model and little deviation is present in between \( t_1 \) and \( t_n \) as in fig. 3(b)

From the above observations, Yamada S-shaped model is more suitable for practical software development environment than NHPP model. This is because one of the NHPP models assumptions is that an immediate effort is taken as soon as faults are identified which is impractical.

As Yamada delayed S-shaped model addresses this issue by considering such delay in its \( m(t) \) and hence the prediction plot has considerable deviation than NHPP model. To have more understanding, the reliability function \( R(t |\delta x) \) is computed for next day \( (\delta x=0.1429 \text{ week}) \) in DS-I and DS-II and for next hour \( (\delta x=0.04167 \text{ day}) \) in DS-III using MATLAB environment. Table 5 & 6 illustrated this performance of both models on three data sets.

Table 5: Reliability Estimation Using NHPP

| NHPP model | \( \lambda(t) \) | \( m(t) \) | \( \lambda(t+\delta x) \) | \( m(t+\delta x) \) | \( R(t|\delta x) \) |
|------------|----------------|----------|-----------------|----------------|-----------------|
| DS – I t=19\( \delta x=0.143 \) | 10.01 | 328 | 9.93 | 329.42 | 0.2407 |
| DS – II t=24\( \delta x=0.143 \) | 1.75 | 84.99 | 2.27 | 85.25 | 0.7791 |
| DS – III t=35\( \delta x=0.042 \) | 0.73 | 73.99 | 0.71 | 74.29 | 0.741 |

Table 6: Reliability Estimation Using Delayed S-Shaped Model

| Yamada S-shaped model | \( \lambda(t) \) | \( m(t) \) | \( \lambda(t+\delta x) \) | \( m(t+\delta x) \) | \( R(t|\delta x) \) |
|-----------------------|----------------|----------|-----------------|----------------|-----------------|
| DS – I t=19\( \delta x=0.143 \) | 5.48 | 327.99 | 5.36 | 328.77 | 0.46 |
| DS – II t=24\( \delta x=0.143 \) | 0.92 | 85 | 0.90 | 85.13 | 0.88 |
| DS – III t=35\( \delta x=0.042 \) | 0.32 | 74 | 0.30 | 74.13 | 0.88 |

Alternately, the reliability is computed numerically as cited in [10]

\[
R^f = 1 - \frac{TNOFR}{TNOF} \\
(17)
\]

Here, TNOFR represents the number residuals and TNOF represents total number of expected faults. The values for both TNOFR and TNOF are obtained by using SMERFS 3.0. Irrespective of the model application (NHPP or S-shaped) and test duration (Weeks/ Days), the reliability is computed numerically and we observe that the higher reliability is obtained for DS-III. Table 7 illustrates the results obtained from SMERFS tool.
Table 7: Reliability Estimation Using Fault Residuals

<table>
<thead>
<tr>
<th>Length</th>
<th>CF</th>
<th>TNOFR</th>
<th>TNOF</th>
<th>RF</th>
</tr>
</thead>
<tbody>
<tr>
<td>DS–I</td>
<td>19</td>
<td>328</td>
<td>157.82</td>
<td>482.82</td>
</tr>
<tr>
<td>DS–II</td>
<td>24</td>
<td>85</td>
<td>30.962</td>
<td>112.96</td>
</tr>
<tr>
<td>DS–III</td>
<td>35</td>
<td>74</td>
<td>12.450</td>
<td>85.450</td>
</tr>
</tbody>
</table>

V. Conclusion

In this paper, three failure data sets have been selected and employed on two Poisson Process based SRGMs for software reliability estimation. First, the three data sets have applied with SMERFS 3.0 and based on its output, the reliability is computed numerically. Then the same data sets have been employed on both NHPP and Delayed S-shaped models. The proportionality constant for each model has been obtained from SMERFS tool, and mean value functions for each model have been plotted using MATLAB environment. In both cases, we have studied that the quality of data set has considerable role in the software reliability estimation. Indeed, our study may motivate the researchers to address the issues on failure data collection and characterization and reveals the possible risks in the initial parameter estimation for any of the SRGM models to be used for software reliability estimation.

References

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